

Review 238

Adding and Subtracting Rational Numbers

To add or subtract fractions and mixed numbers with unlike denominators, first rewrite the fractions using the least common denominator (LCD).

Subtract: $2\frac{3}{4} - 5\frac{1}{3}$

$$2\frac{3}{4} - 5\frac{1}{3} = \frac{11}{4} - \frac{16}{3}$$

$$= \frac{33}{12} - \frac{64}{12} \quad \leftarrow \text{The LCD is 12.}$$

$$= \frac{-31}{12} \quad \leftarrow \text{Subtract numerators.}$$

$$= -2\frac{7}{12} \quad \leftarrow \text{Simplify.}$$

$$2\frac{3}{4} - 5\frac{1}{3} = -2\frac{7}{12}$$

You can use addition or subtraction to solve equations with rational numbers.

Solve: $h - \frac{3}{8} = \frac{1}{6}$

$$h - \frac{3}{8} + \frac{3}{8} = \frac{1}{6} + \frac{3}{8} \quad \leftarrow \text{Add } \frac{3}{8}.$$

$$h = \frac{4}{24} + \frac{9}{24} \quad \leftarrow \text{The LCD is 24.}$$

$$h = \frac{13}{24}$$

Find each sum or difference as a fraction or mixed number in simplest form.

1. $6\frac{1}{4} - 2\frac{3}{8}$

2. $\frac{5}{6} + (-\frac{1}{2})$

3. $-4\frac{1}{3} - (-\frac{3}{5})$

4. $\frac{1}{8} - (-\frac{1}{6})$

5. $-1\frac{3}{8} - 4\frac{1}{12}$

6. $\frac{7}{10} + (-\frac{12}{5})$

7. $1\frac{5}{8} - (-2\frac{1}{2})$

8. $-2\frac{1}{3} - (-1\frac{5}{12})$

9. $-10 - (3\frac{11}{12})$

10. $1\frac{1}{3} - 4\frac{3}{4}$

11. $9 + (-6\frac{5}{9})$

12. $-2\frac{5}{6} - 5\frac{5}{12}$

Solve each equation. Write each answer as a mixed number or as a fraction in simplest form.

13. $y + \frac{7}{8} = -\frac{1}{4}$

14. $c + -\frac{3}{5} = \frac{1}{2}$

15. $m - 3\frac{2}{3} = 1\frac{1}{6}$

16. $x - 2\frac{1}{4} = -3$

17. $n + \frac{1}{2} = -2\frac{5}{6}$

18. $\frac{1}{2} + d = -3\frac{1}{5}$

19. $7.3 + g = 1\frac{4}{5}$

20. $y - 4.1 = 2\frac{3}{4}$

21. $z + 2.6 = 0.37$

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Multiplying and Dividing Rational Numbers

To multiply rational numbers in fraction form, multiply numerators, then multiply denominators.

Multiply: $\frac{7}{12} \cdot 1\frac{4}{5}$
 $\frac{7}{12} \cdot \frac{9}{5}$ ← fraction form
 $\frac{7 \cdot 9}{12 \cdot 5}$ ← Multiply numerators.
 $\frac{7 \cdot 9}{12 \cdot 5}$ ← Multiply denominators.
 $\frac{63}{60} = 1\frac{3}{60} = 1\frac{1}{20}$ ← Simplify.

To divide, multiply by the reciprocal of the divisor.

Divide: $-3\frac{1}{8} \div \frac{2}{3}$
 $\frac{-25}{8} \div \frac{2}{3}$ ← fraction form
 $\frac{-25}{8} \cdot \frac{3}{2}$ ← reciprocal of divisor
 $\frac{-25 \cdot 3}{8 \cdot 2} = \frac{-75}{16}$ ← Multiply.
 $= -4\frac{11}{16}$ ← Simplify.

Find each product. Write each answer as a fraction or mixed number in simplest form.

1. $\frac{8}{9} \cdot (-\frac{3}{4})$

2. $-\frac{1}{2} \cdot \frac{4}{5}$

3. $-\frac{2}{3} \cdot (-\frac{1}{8})$

4. $\frac{5}{6} \cdot \frac{3}{7}$

5. $\frac{3}{4} \cdot (-\frac{2}{3})$

6. $3 \cdot 2\frac{1}{4}$

7. $-5\frac{1}{2} \cdot 1\frac{3}{4}$

8. $-2\frac{1}{8} \cdot (-3)$

9. $4\frac{1}{5} \cdot 2\frac{1}{2}$

10. $\frac{13}{15} \cdot \frac{5}{6}$

11. $-3\frac{2}{5} \cdot 2\frac{1}{2}$

12. $-5 \cdot (-2\frac{1}{4})$

13. $-\frac{5}{8} \cdot 4\frac{2}{3}$

14. $-5 \cdot 3\frac{3}{10}$

15. $-2\frac{3}{5} \cdot (-3\frac{1}{3})$

Find each quotient.

16. $\frac{5}{6} \div \frac{3}{5}$

17. $-\frac{3}{8} \div (-\frac{1}{2})$

18. $-6 \div \frac{3}{4}$

19. $4 \div (-\frac{2}{3})$

20. $5\frac{1}{4} \div 1\frac{1}{2}$

21. $1\frac{1}{4} \div (-\frac{2}{5})$

22. $-\frac{3}{4} \div (-1\frac{1}{2})$

23. $-1\frac{3}{5} \div \frac{1}{4}$

24. $2\frac{1}{2} \div \frac{3}{10}$

25. $-\frac{5}{9} \div (-\frac{2}{3})$

26. $-6 \div 3\frac{5}{8}$

27. $\frac{3}{4} \div (-9)$

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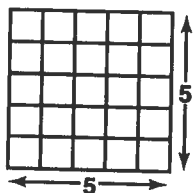
Exploring Square Roots and Irrational Numbers

The square of 5 is 25.

$$5 \cdot 5 = 5^2 = 25$$

The *square root* of 25 is 5 because $5^2 = 25$.

$$\sqrt{25} = 5$$



$1^2 = 1$	} <i>perfect squares</i>
$2^2 = 4$	
$3^2 = 9$	
$4^2 = 16$	
$5^2 = 25$	

You can use a calculator to find square roots.

Example: Find $\sqrt{36}$ and $\sqrt{21}$ to the nearest tenth.

$$36 \sqrt{\square} = 6 \quad 21 \sqrt{\square} \approx 4.5825757 \approx 4.6$$

You can estimate square roots like $\sqrt{52}$ and $\sqrt{61}$.

Perfect squares	↗ 49		$\sqrt{49} = 7$		$\sqrt{49} = 7$
	52	Estimate	$\sqrt{52} \approx 7$	Estimate	$\sqrt{61} \approx 8$
	↘ 64		$\sqrt{64} = 8$		$\sqrt{64} = 8$

Find each square root. Round to the nearest integer if necessary. Use \approx to show that a value is rounded.

- | | | | |
|---------------------------|---------------------------|---------------------------|---------------------------|
| 1. $\sqrt{16}$
_____ | 2. $\sqrt{85}$
_____ | 3. $\sqrt{26}$
_____ | 4. $\sqrt{36}$
_____ |
| 5. $\sqrt{98}$
_____ | 6. $\sqrt{40}$
_____ | 7. $\sqrt{100}$
_____ | 8. $\sqrt{18}$
_____ |
| 9. $\sqrt{5}$
_____ | 10. $\sqrt{121}$
_____ | 11. $\sqrt{68}$
_____ | 12. $\sqrt{144}$
_____ |
| 13. $\sqrt{29}$
_____ | 14. $\sqrt{64}$
_____ | 15. $\sqrt{37}$
_____ | 16. $\sqrt{75}$
_____ |
| 17. $\sqrt{225}$
_____ | 18. $\sqrt{54}$
_____ | 19. $\sqrt{169}$
_____ | 20. $\sqrt{103}$
_____ |
| 21. $\sqrt{61}$
_____ | 22. $\sqrt{400}$
_____ | 23. $\sqrt{119}$
_____ | 24. $\sqrt{84}$
_____ |

25. If a whole number is not a perfect square, its square root is an *irrational number*. List the numbers from Exercises 1–24 that are irrational.

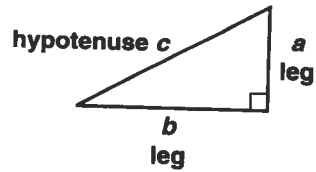
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The Pythagorean Theorem

The Pythagorean Theorem

The sum of the squares of the lengths of the legs of a right triangle is equal to the square of the length of the hypotenuse.

Also, if $a^2 + b^2 = c^2$, then the triangle is a right triangle.



$$a^2 + b^2 = c^2$$

Example 1: Find the length of a leg of a right triangle if the length of the other leg is 12 cm and the length of the hypotenuse is 13 cm.

$$\begin{aligned} a^2 + b^2 &= c^2 \\ 12^2 + b^2 &= 13^2 \\ 144 + b^2 &= 169 \\ 144 - 144 + b^2 &= 169 - 144 \\ b^2 &= 25 \\ b &= \sqrt{25} \\ b &= 5 \end{aligned}$$

The length of the leg is 5 cm.

Example 2: Is a triangle with sides 6 m, 7 m, and 10 m a right triangle?

$$\begin{aligned} a^2 + b^2 &= c^2 \\ 6^2 + 7^2 &\stackrel{?}{=} 10^2 && \leftarrow \text{Substitute.} \\ 36 + 49 &\stackrel{?}{=} 100 && \leftarrow \text{Simplify.} \\ 85 &\neq 100 \end{aligned}$$

The triangle is *not* a right triangle.

The lengths of two sides of a right triangle are given. Find the length of the third side.

1. legs: 6 ft and 8 ft
hypotenuse:

2. leg: 15 m
hypotenuse: 17 m
leg:

3. leg: 12 in.
hypotenuse: 15 in.
leg:

4. leg: 1.5 km
hypotenuse: 2.5 km
leg:

5. legs: 15 in. and 20 in.
hypotenuse:

6. leg: 16 m
hypotenuse: 34 m
leg:

Is a triangle with the given side lengths a right triangle?

7. 10 cm, 24 cm, 26 cm

8. 5 ft, 7 ft, 9 ft

9. 6 m, 12 m, 15 m

10. 5 in., 12 in., 13 in.

11. 30 mm, 40 mm, 50 mm

12. 2 yd, 5 yd, 8 yd

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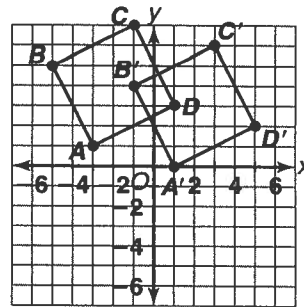
Translations

Movements of figures on a plane are called **transformations**. A translation, or slide, moves all points the same distance and direction.

The translation $(x, y) \rightarrow (x + 4, y - 1)$ moves *each* point to the right 4 units and down 1 unit.

$A(-3, 1)$ moves to $(-3 + 4, 1 - 1)$, where point $A'(1, 0)$ is its **image**.

The square $ABCD$ moves to its image square $A'B'C'D'$.

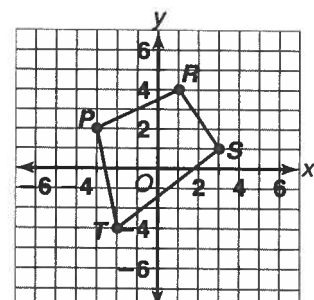
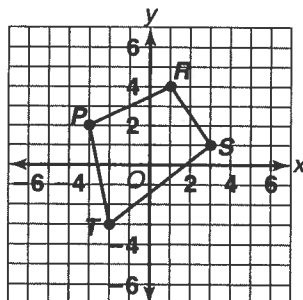
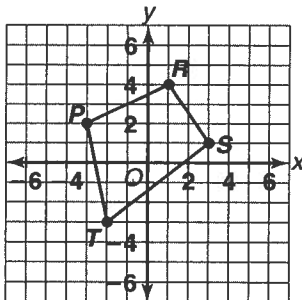


Complete the following for the figure above.

1. $B(-5, 5) \rightarrow B'(\underline{\hspace{1cm}}, \underline{\hspace{1cm}})$
2. $C(-1, 7) \rightarrow C'(\underline{\hspace{1cm}}, \underline{\hspace{1cm}})$
3. $D(\underline{\hspace{1cm}}, \underline{\hspace{1cm}}) \rightarrow D'(\underline{\hspace{1cm}}, \underline{\hspace{1cm}})$

Graph each translation of figure $PRST$.

4. right 2 units
5. left 2 units, down 2 units
6. right 1 unit, up 3 units



Complete the rule for each translation.

7. right 3 units, up 1 unit
 $(x, y) \rightarrow \underline{\hspace{2cm}}$
8. left 4 units, up 5 units
 $(x, y) \rightarrow \underline{\hspace{2cm}}$
9. left 1 unit, down 9 units
 $(x, y) \rightarrow \underline{\hspace{2cm}}$

Write a rule for the translation.

10. left 1 unit, down 3 units
 $\underline{\hspace{2cm}}$
11. right 1 unit, up 2 units
 $\underline{\hspace{2cm}}$
12. left 3 units, up 2 units
 $\underline{\hspace{2cm}}$

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Translations

A *translation* moves every point of a figure the same distance in the same direction.

Triangle ABC is translated 5 units to the right and 4 units up. The *image* of $\triangle ABC$ is $\triangle A'B'C'$.

You can write a rule to describe a translation in the coordinate plane.

For the translation of $\triangle DEF$, the rule is:

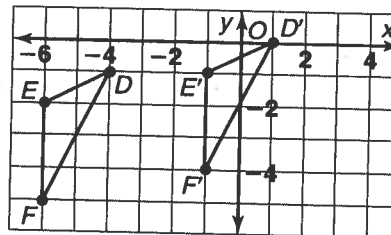
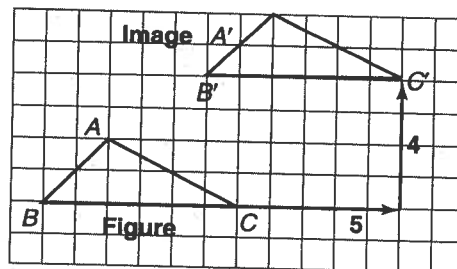
Add 5 to each x -coordinate.

Add 1 to each y -coordinate.

$$D(-4, -1) \rightarrow D'(1, 0)$$

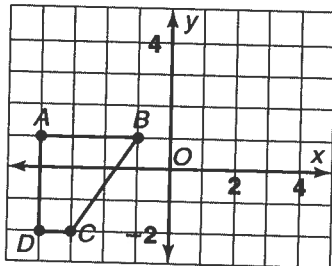
$$E(-6, -2) \rightarrow E'(-1, -1)$$

$$F(-6, -5) \rightarrow F'(-1, -4)$$

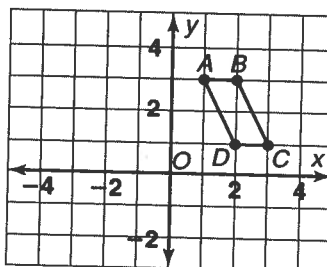


Copy each figure. Then graph the image after the given translation. Name the coordinates of the image.

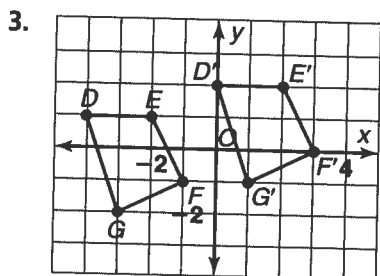
1. right 5 units, up 1 unit

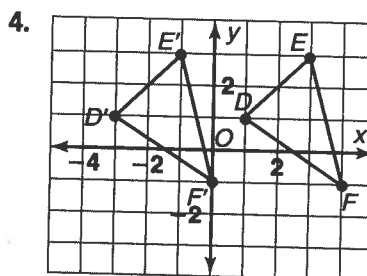


2. left 3 units, down 2 units



Use arrow notation to write a rule that describes the translation shown on each graph.





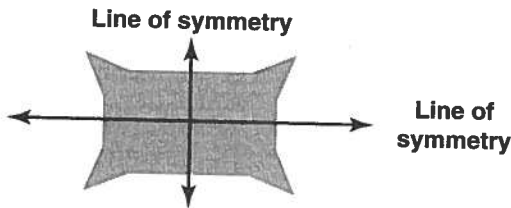
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Symmetry and Reflections

Symmetry

A figure is **symmetrical** if one side is a mirror image of the other. The line that divides a figure into two identical parts is called a **line of symmetry**.

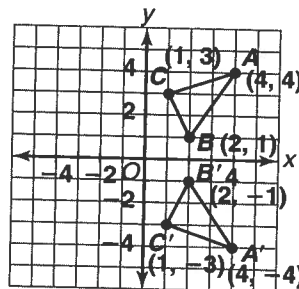
The figure below has 2 lines of symmetry.



You can trace the figure and fold it along either line to see that the two halves match.

Reflections

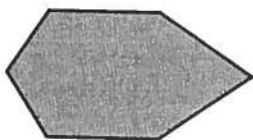
A **reflection** is a transformation that creates a mirror image. $\triangle A'B'C'$ is the mirror image of $\triangle ABC$ across the x -axis. The x -axis is the **line of reflection**.



- When you reflect across the x -axis, the y -coordinates change sign.
- When you reflect across the y -axis, the x -coordinates change sign.
- When you reflect across a line of symmetry, the image is the figure itself.

Draw the line(s) of symmetry. If there are no lines of symmetry, write *none*.

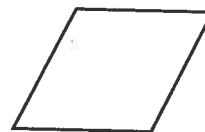
1.



2.



3.



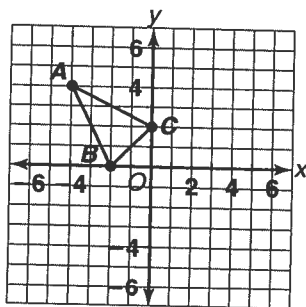
$\triangle ABC$ is shown. Draw $\triangle A'B'C'$ so it is a reflection of $\triangle ABC$ over the specified axis. Then complete each statement.

4. over the x -axis

$A(-4, 4) \rightarrow A'$

$B(-2, 0) \rightarrow B'$

$C(0, 2) \rightarrow C'$

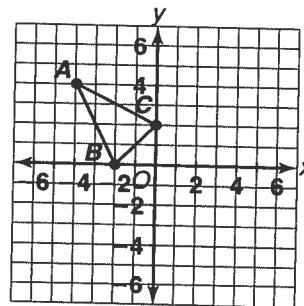


5. over the y -axis

$A(-4, 4) \rightarrow A'$

$B(-2, 0) \rightarrow B'$

$C(0, 2) \rightarrow C'$



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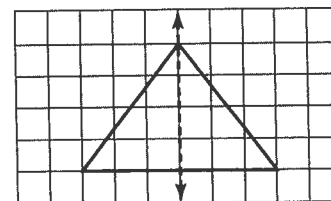
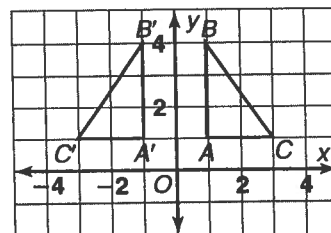
Reflections and Symmetry

A *reflection* flips a figure over a line (the *line of reflection*). Figure $A'B'C'$ is the image of figure ABC after a reflection over the y -axis.

Each point of the image is the same distance from the line of reflection as the corresponding point of the original figure.

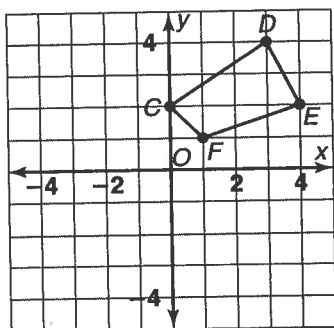
Since A is 1 unit to the right of the y -axis, locate A' 1 unit to the left of the y -axis.

If the image is identical to the original figure, then the figure has *reflectional symmetry* and has a *line of symmetry*.

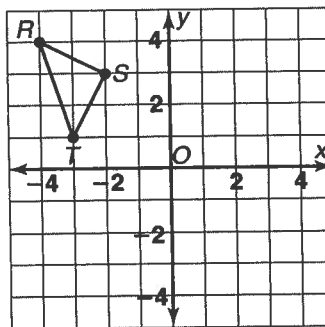


Copy each figure.

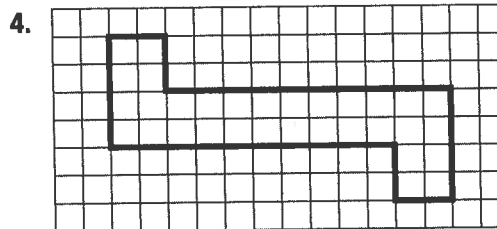
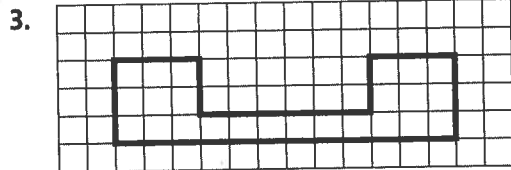
1. Reflect the figure over the x -axis.



2. Reflect the figure over the y -axis.



Copy each figure. Does the figure have reflectional symmetry? If it does, draw all the lines of symmetry.



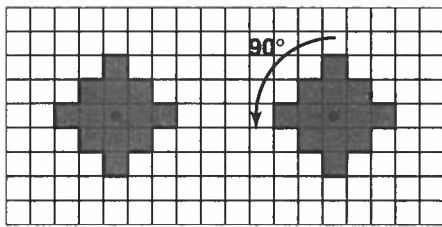
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Rotations

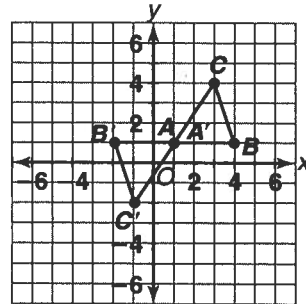
A **rotation** is a transformation that turns a figure about a fixed point. The fixed point is called the **center of rotation**.

A figure has **rotational symmetry** if it can be rotated less than 360° and fit exactly on top of the original figure.

The figure below has rotational symmetry.



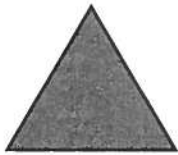
To draw a 180° rotation about point A , trace $\triangle ABC$. Place a pencil tip on point A and rotate the tracing 180° . Mark points A' , B' , and C' . Then draw $\triangle A'B'C'$.



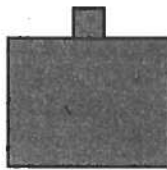
For a rotation of 90° or 180° about its center, the figure fits exactly on top of itself.

Does each figure have rotational symmetry?

1.



2.

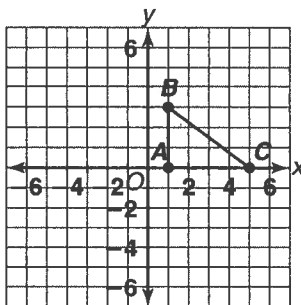


3.

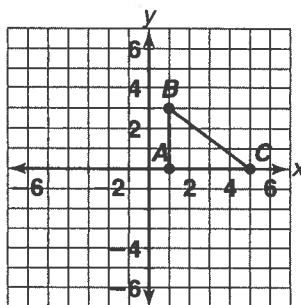


Draw the image of the figure after each rotation about point O .

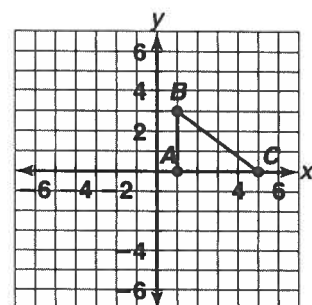
4. rotation of 90°



5. rotation of 180°



6. rotation of 270°



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Rotations

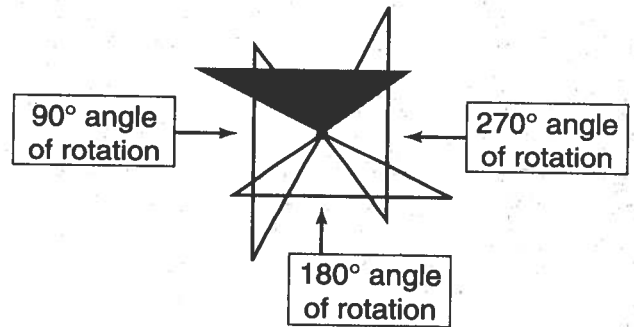
A *rotation* is a turn of a figure about a center point, the *center of rotation*.

A figure can be rotated up to 360° counterclockwise.

A figure has *rotational symmetry* if an image matches the original figure after a rotation of 180° or less.

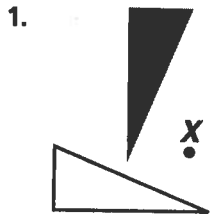
The angle measure the figure rotates is the *angle of rotation*.

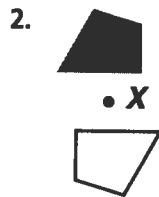
The shaded triangle is rotated about its lower vertex.

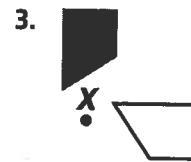


The triangle does not have rotational symmetry.

The shaded figure is rotated 90° , 180° , or 270° about point X . The unshaded figure is its image. What is the angle of rotation?



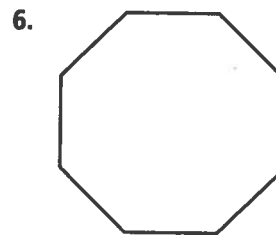




Judging by appearance, determine whether each figure has rotational symmetry. If it does, find the angle of rotation.





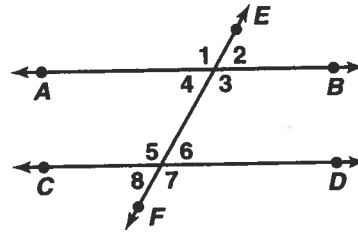


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Angles and Parallel Lines

Look at the figure at the right.

- Line \overleftrightarrow{AB} is parallel to line \overleftrightarrow{CD} ($\overleftrightarrow{AB} \parallel \overleftrightarrow{CD}$)
- Line \overleftrightarrow{EF} is a transversal.



Alternate interior angles lie within a pair of lines and on opposite sides of the transversal.

Example 1: $\angle 3$ and $\angle 5$, $\angle 4$ and $\angle 6$

Alternate interior angles are congruent. If $m\angle 4$ is 60° , then $m\angle 6$ is also 60° .

Corresponding angles lie on the same side of the transversal and in corresponding positions.

Example 2: $\angle 1$ and $\angle 5$, $\angle 3$ and $\angle 7$

Corresponding angles are congruent. If $m\angle 1$ is 120° , then $m\angle 5$ is also 120° .

Use the diagram at the right to complete Exercises 1–2.

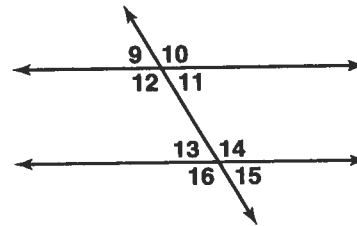
1. Name the alternate interior angles.

- a. $\angle 11$ and $\angle \underline{\quad ? \quad}$ b. $\angle 12$ and $\angle \underline{\quad ? \quad}$

2. Name the corresponding angles.

- a. $\angle 16$ and $\angle \underline{\quad ? \quad}$ b. $\angle 14$ and $\angle \underline{\quad ? \quad}$

- c. $\angle 9$ and $\angle \underline{\quad ? \quad}$ d. $\angle 11$ and $\angle \underline{\quad ? \quad}$

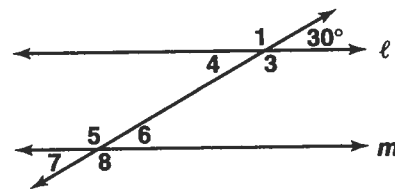


In the diagram at the right, $\ell \parallel m$. Find the measure of each angle.

3. $\angle 1$ 4. $\angle 3$

5. $\angle 6$ 6. $\angle 5$

7. $\angle 8$ 8. $\angle 7$



Review 274

Areas of Polygons

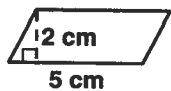
Example 1: Find the area of the parallelogram. Use the formula below.

Area = base \times height

$$A = bh$$

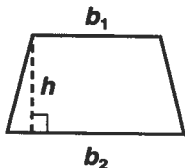
$$= 5 \times 2$$

$$= 10 \text{ cm}^2$$



The area of a trapezoid is half the product of the height and the sum of the lengths of the bases.

$$A = \frac{1}{2}h(b_1 + b_2)$$



Example 2: Find the area of the triangle. You can cut a parallelogram into two congruent triangles. So, the area of a triangle is half the area of a parallelogram.

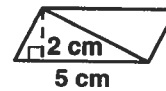
To find the area of a triangle, use this formula.

Area = $\frac{1}{2}$ base \times height

$$A = \frac{1}{2}bh$$

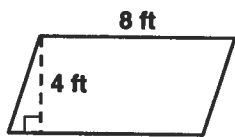
$$= \frac{1}{2} \times 5 \times 2$$

$$= 5 \text{ cm}^2$$



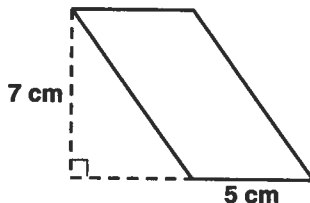
Find the area of each parallelogram.

1.



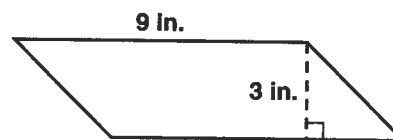
$$A = \underline{\hspace{2cm}}$$

2.



$$A = \underline{\hspace{2cm}}$$

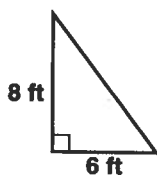
3.



$$A = \underline{\hspace{2cm}}$$

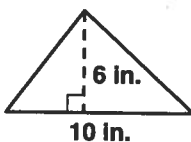
Find the area of each triangle.

4.



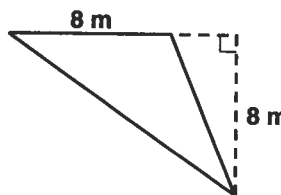
$$A = \underline{\hspace{2cm}}$$

5.



$$A = \underline{\hspace{2cm}}$$

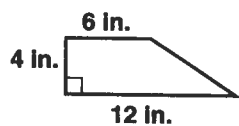
6.



$$A = \underline{\hspace{2cm}}$$

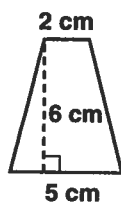
Find the area of each trapezoid.

7.



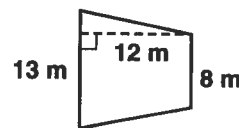
$$A = \underline{\hspace{2cm}}$$

8.



$$A = \underline{\hspace{2cm}}$$

9.



$$A = \underline{\hspace{2cm}}$$

Review 275

Circumferences and Areas of Circles

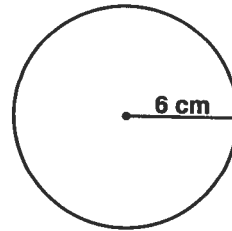
The distance around a circle is called the *circumference*.

- You can use a formula to find the circumference (C) of a circle. Pi (π) is approximately equal to (\approx) 3.14.

$$\begin{aligned} \text{Circumference} &= 2 \times \pi \times \text{radius} \\ C &= 2\pi r \end{aligned}$$

- If you know the diameter, use this formula:

$$\begin{aligned} \text{Circumference} &= \pi \times \text{diameter} \\ C &= \pi d \end{aligned}$$



$$\begin{aligned} \text{Circumference} &= 2 \times \pi \times r \\ C &= 2 \times \pi \times 6 \\ &\approx 37.7 \text{ cm} \end{aligned}$$

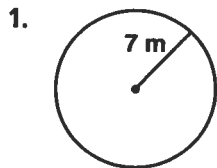
To find the *area of a circle*, use this formula:

$$\begin{aligned} \text{Area} &= \pi \times \text{radius}^2 \\ A &= \pi r^2 \end{aligned}$$

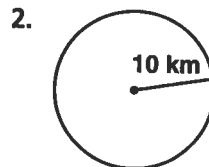
$$\begin{aligned} \text{Area} &= \pi \times r^2 \\ A &= \pi \times 6^2 \\ &\approx 113.1 \text{ cm}^2 \end{aligned}$$

The circumference of the circle is about 37.7 cm. The area of the circle is about 113.1 cm².

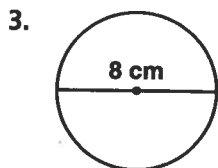
Find the circumference and area of each circle. Round to the nearest tenth.



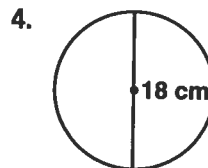
$$C \approx \underline{\hspace{2cm}} \quad A \approx \underline{\hspace{2cm}}$$



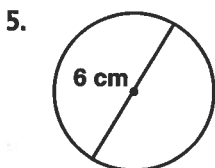
$$C \approx \underline{\hspace{2cm}} \quad A \approx \underline{\hspace{2cm}}$$



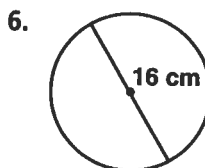
$$C \approx \underline{\hspace{2cm}} \quad A \approx \underline{\hspace{2cm}}$$



$$C \approx \underline{\hspace{2cm}} \quad A \approx \underline{\hspace{2cm}}$$



$$C \approx \underline{\hspace{2cm}} \quad A \approx \underline{\hspace{2cm}}$$

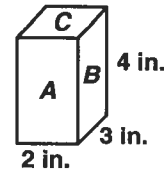


$$C \approx \underline{\hspace{2cm}} \quad A \approx \underline{\hspace{2cm}}$$

Review 280

Surface Areas of Prisms and Cylinders

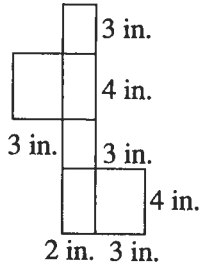
The *surface area* of a solid is the sum of the areas of its surfaces. S.A. stands for *surface area* and L.A. stand for *lateral area*.



Example 1: Find the surface area of the prism.

Using a Net to Find Surface Area of a Prism

Draw a net of the prism and find the area of each rectangle in the net.



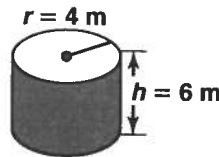
$$\begin{aligned} \text{S.A.} &= \\ (2 \cdot 3) &+ (2 \cdot 3) + (3 \cdot 4) + (3 \cdot 4) + (2 \cdot 4) + (2 \cdot 4) \\ &= 6 + 6 + 12 + 12 + 8 + 8 \\ &= 52 \text{ in.}^2 \end{aligned}$$

Using the Prism Surface Area Formula

The lateral area of a prism is the product of the perimeter of the base and the height of the prism.

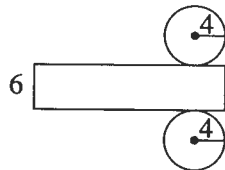
$$\begin{aligned} \text{L.A.} &= ph \\ \text{S.A.} &= \text{L.A.} + 2B \\ &= ph + 2B \\ &= (2 + 2 + 3 + 3)4 + 2(2 \cdot 3) \\ &= 10(4) + 2(6) \\ &= 40 + 12 = 52 \text{ in.}^2 \end{aligned}$$

Example 2: Find the surface area of the cylinder.



Using a Net to Find Surface Area of a Cylinder

Draw a net of the cylinder and find the area of each shape in the net.

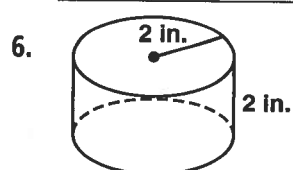
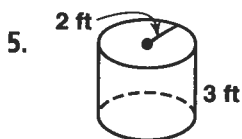
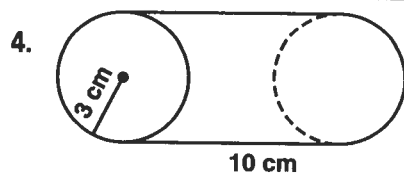
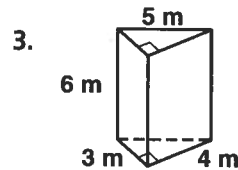
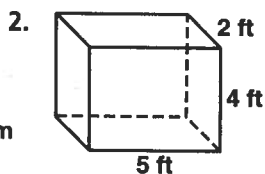
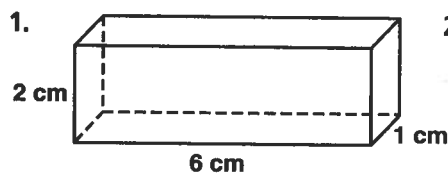


$$\begin{aligned} \text{S.A.} &= 16\pi + 16\pi + 48\pi \\ &= 80\pi \\ &\approx 251.33 \end{aligned}$$

Using the Cylinder Surface Area Formula

$$\begin{aligned} \text{S.A.} &= 2\pi rh + 2\pi r^2 \\ &= 2\pi(4)(6) + 2\pi(4^2) \\ &= 48\pi + 32\pi \\ &= 80\pi \\ &\approx 251.33 \end{aligned}$$

Find the lateral and surface area of each figure to the nearest whole unit.



Review 281

Surface Areas of Pyramids and Cones

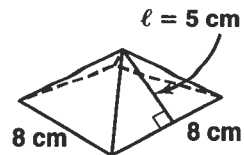
Example 1: Find the surface area of the prism.

The lateral area of a square pyramid is four times the area of one of the lateral faces.

$$\text{L.A.} = 4 \cdot \left(\frac{1}{2}b\ell\right) = 2b\ell$$

The surface area of a square pyramid is the sum of the lateral area and the area of the base.

$$\begin{aligned} \text{S.A.} &= \text{L.A.} + B \\ &= 2b\ell + b^2 \\ &= 2(8)(5) + 8^2 \\ &= 80 + 64 \\ &= 144 \text{ cm}^2 \end{aligned}$$

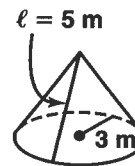


Example 2: Find the surface area of the cone.

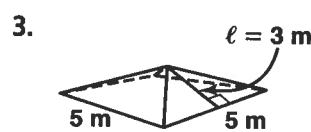
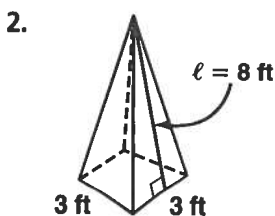
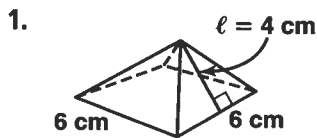
The lateral area of a cone is one half the product of the circumference of the base and the slant height.

$$\text{L.A.} = \frac{1}{2}(2\pi r)\ell = \pi r\ell$$

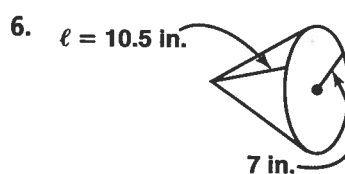
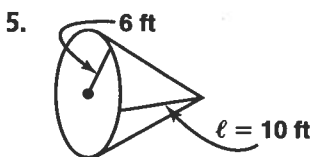
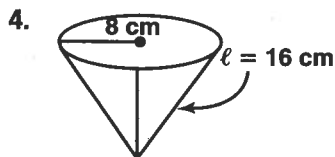
$$\begin{aligned} \text{S.A.} &= \text{L.A.} + B \\ &= \pi r\ell + \pi r^2 \\ &= \pi(3)(5) + \pi(3^2) \\ &= 15\pi + 9\pi \\ &= 24\pi \approx 75.4 \text{ m}^2 \end{aligned}$$



Find the lateral and surface area of each square pyramid.



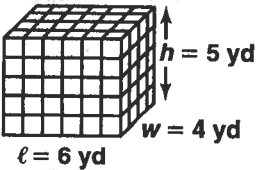
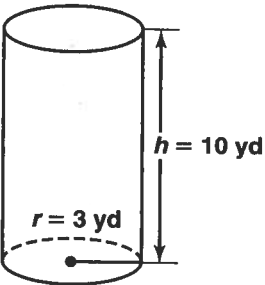
Find the surface area of each cone to the nearest whole unit.



Review 282

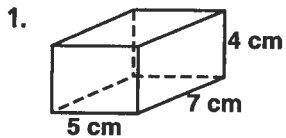
Volumes of Prisms and Cylinders

To find the volume of a prism or a cylinder, multiply the base area B and the height h .

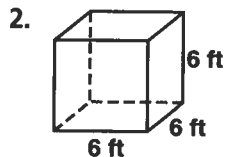
	① Find the base area B .	② Multiply base area B and height h . $V = Bh$
 <p>$l = 6 \text{ yd}$ $w = 4 \text{ yd}$ $h = 5 \text{ yd}$</p>	$B = \ell w$ $= 6 \cdot 4$ $= 24 \text{ yd}^2$	$V = Bh$ $= 24 \cdot 5$ $= 120 \text{ yd}^3$ <p>The volume is 120 yd^3.</p>
 <p>$r = 3 \text{ yd}$ $h = 10 \text{ yd}$</p>	$B = \pi r^2$ $= \pi \cdot 3^2$ $\approx 28.27 \text{ yd}^2$	$V = Bh$ $\approx 28.27 \cdot 10$ $\approx 282.7 \text{ yd}^3$ <p>The volume is about 283 yd^3.</p>

Course 3 Topics

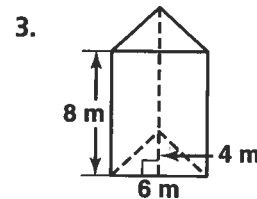
Find the base area and volume of each prism.



$B =$ _____
 $V =$ _____

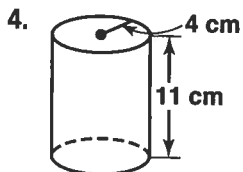


$B =$ _____
 $V =$ _____

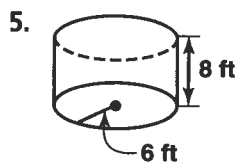


$B =$ _____
 $V =$ _____

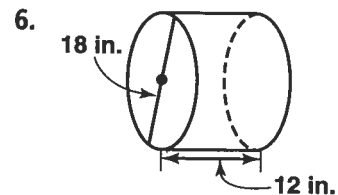
Find the base area of each cylinder to the nearest hundredth. Then find the volume of each cylinder to the nearest whole unit.



$B \approx$ _____
 $V \approx$ _____



$B \approx$ _____
 $V \approx$ _____

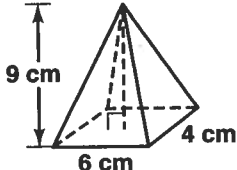
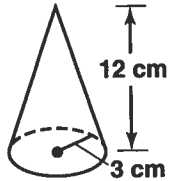


$B \approx$ _____
 $V \approx$ _____

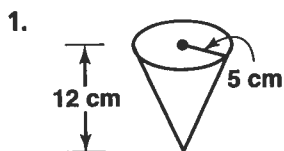
Review 283

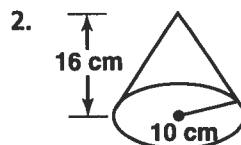
Volumes of Pyramids and Cones

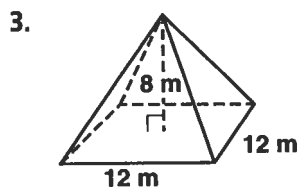
To find the volume of a pyramid or cone, multiply $\frac{1}{3}$, the base area B , and the height h .

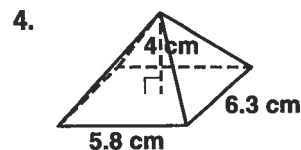
	① Find the base area B .	② Multiply $\frac{1}{3}$, the base area B , and the height h . $V = \frac{1}{3}Bh$
	$B = \ell w$ $= 6 \cdot 4$ $= 24 \text{ cm}^2$	$V = \frac{1}{3}Bh$ $= \frac{1}{3}(24)(9)$ $= 72 \text{ cm}^3$ <p>The volume is 72 cm^3.</p>
	$B = \pi r^2$ $= \pi \cdot 3^2$ $\approx 28.27 \text{ cm}^2$	$V = \frac{1}{3}Bh$ $\approx \frac{1}{3}(28.27)(12)$ $\approx 113.08 \text{ cm}^3$ <p>The volume is about 113.08 cm^3.</p>

Find the volume of each figure to the nearest whole unit.









5. Find the height of a cone with an approximate volume of 134 cm^3 and a radius of 4 cm.
